

## Vibrational Analysis of the Radical Anion and Cation of Biphenyl Based on Density Functional Calculations

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The density functional theory has been used for calculating the structures and vibrational wavenumbers of the radical anion and cation of biphenyl. The radical anion has a planar structure, while the radical cation is twisted. Upon ionization, structural changes occur in the direction from benzenoid to quinoid. Unscaled wavenumbers calculated at the Becke-Lee-Yang-Parr/6-31G\* level are mostly in agreement with observed vibrational wavenumbers in the literature.

Poly(*p*-phenylene) (PPP) is one of conducting polymers,<sup>1</sup> which has received much attention from viewpoints of pure and applied sciences. PPP shows high electrical conductivities when oxidized with acceptors or reduced with donors, while it is an insulator in the undoped state.<sup>2</sup> Its high conductivities have been interpreted in terms of polarons and bipolarons, which are elementary excitations in nondegenerate conjugated polymers such as PPP.<sup>1</sup> A positive (negative) polaron and a positive (negative) bipolaron correspond to a radical cation (radical anion) and a dication (dianion), respectively.

The Raman spectra of Na-doped PPP have been analyzed on the basis of the Raman spectra of the radical anions and dianions of *p*-oligophenyls, and it has been concluded that negative polarons and bipolarons are formed in Na-doped PPP.<sup>3</sup> Theoretical studies of the radical ions (polaron models) and divalent ions (bipolaron models) of *p*-oligophenyls are thus useful for characterizing polarons and bipolarons in PPP. The structures of the divalent ions of *p*-oligophenyls consisting of up to 11 rings have been calculated by using the *ab initio* Hartree-Fock (HF) method.<sup>4-6</sup> However, treatments incorporating electron correlation are required for a correct understanding of polarons and bipolarons in conjugated systems.<sup>1,7</sup> Rubio *et al.*<sup>8</sup> have studied the structures of the radical anion and cation of biphenyl using the complete active space self-consistent field (CASSCF) method. It is practically impossible to calculate the vibrational wavenumbers of the radical ions and divalent ions of long-chain *p*-oligophenyls at such a high theoretical level. As an alternative, the density functional theory (DFT) may be used, since it has the ability to incorporate electron correlation in treating quite large molecules and charged species. In this letter, we apply the DFT approach to studies on the structures and vibrational spectra of the radical anion and cation of biphenyl, which is the smallest of *p*-oligophenyls, in order to evaluate the usefulness of the DFT approach in studying charged species of longer *p*-oligophenyls.

The structures and harmonic vibrational wavenumbers were calculated for biphenyl and its radical anion and cation. Counter ions were not included in the calculations of the radical ions. Density functional calculations were performed by using the Gaussian 92/DFT program<sup>9</sup> on a Kubota Titan 3000 computer and a Silicon Graphics Power Onyx workstation. The 6-31G\* and 6-311G\* basis sets were used. Two sets of calculations were carried out with the following functionals, *i.e.*, (i) Becke's

**Table 1.** Torsional angles and CC bond lengths calculated at the BLYP/6-31G\* level for biphenyl and its radical ions

Parameter	Angles / ° and bond lengths / Å		
	Neutral	Radical anion	Radical cation
$\tau(C_2C_1C_1'C_2')$	38.4	0	18.7
$r(C_1C_1')$	1.494	1.451	1.458
$r(C_1C_2)$	1.416	1.451	1.443
$r(C_2C_3)$	1.404	1.394	1.390
$r(C_3C_4)$	1.406	1.421	1.418

exchange functional<sup>10</sup> in combination with the Lee-Yang-Parr correlation functional<sup>11</sup> (BLYP) and (ii) Becke's three-parameter hybrid method<sup>12</sup> using the Lee-Yang-Parr correlation functional<sup>11</sup> (B3LYP) as implemented in the Gaussian 92/DFT program. The default grid was used for numerical evaluation of two-electron integrals. Geometry optimizations were performed under  $D_2$  symmetry for biphenyl and its radical ions. Since an almost planar structure was obtained for the radical anion, the geometry optimization of this species was finally performed under  $D_{2h}$  symmetry. No imaginary-frequency mode was found at the optimized structures of all the species.

The torsional angles and CC bond lengths calculated at the BLYP/6-31G\* level for biphenyl and its radical ions are shown in Table 1. Biphenyl in the neutral state has a twisted structure ( $D_2$  symmetry); the torsional angles around the inter-ring  $C_1C_1'$  bond calculated at the BLYP/6-31G\*, BLYP/6-311G\*, B3LYP/6-31G\*, and B3LYP/6-311G\* levels are 38.4, 41.9, 39.3, and 42.2°, respectively. The torsional angle in the vapor phase has been determined to be 44.4° by means of electron diffraction.<sup>13</sup> The calculated structure of the radical anion is planar ( $D_{2h}$  symmetry). On the other hand, the radical cation has a twisted structure ( $D_2$  symmetry); the torsional angles calculated at the BLYP/6-31G\*, BLYP/6-311G\*, B3LYP/6-31G\*, and B3LYP/6-311G\* levels are 18.7, 20.1, 16.8, and 16.9°, respectively. In a study of the Raman spectra of the radical anion and cation in solutions, Sasaki and Hamaguchi<sup>14</sup> have proposed that the radical cation is slightly twisted, whereas the radical anion is planar. Rubio *et al.*<sup>8</sup> have reported a planar structure for the radical cation, because they have optimized its geometry with the constraint of  $D_{2h}$  symmetry. The CC bond lengths of biphenyl and its radical ions depend on the exchange and correlation functionals rather than the basis sets. Except for the  $C_1C_1'$  bond, the CC bond lengths calculated by the B3LYP method are in agreement with those calculated by the CASSCF method,<sup>8</sup> while those calculated by the BLYP method are longer by about 0.01 Å. The calculated length of the  $C_1C_1'$  bond varies with the theoretical level to a greater extent. As shown in Table 1, the  $C_1C_1'$  and  $C_2C_3$  bonds are shortened and the  $C_1C_2$  and

**Table 2.** Calculated and observed vibrational wavenumbers of biphenyl and its radical ions

Neutral			Radical anion			Radical cation		
Mode	Obs <sup>b</sup>	Calc <sup>a</sup>	Mode	Obs <sup>c</sup>	Calc <sup>a</sup>	Mode	Obs <sup>d</sup>	Calc <sup>a</sup>
	cm <sup>-1</sup>	cm <sup>-1</sup>		cm <sup>-1</sup>	cm <sup>-1</sup>		cm <sup>-1</sup>	cm <sup>-1</sup>
<i>a</i> v <sub>4</sub>	1613	1595	<i>a<sub>g</sub></i> v <sub>4</sub>	1587	1604	<i>a</i> v <sub>4</sub>	1615	1607
v <sub>5</sub>	1505	1508	<i>a<sub>g</sub></i> v <sub>5</sub>	1493	1495	v <sub>5</sub>	1502	1490
v <sub>6</sub>	1282	1268	<i>a<sub>g</sub></i> v <sub>6</sub>	1326	1312	v <sub>6</sub>	1342	1307
v <sub>7</sub>	1192	1194	<i>a<sub>g</sub></i> v <sub>7</sub>	1201	1215	v <sub>7</sub>	1224	1225
v <sub>8</sub>	1029	1031	<i>a<sub>g</sub></i> v <sub>8</sub>	1017	1003	v <sub>8</sub>	1018	1012
v <sub>9</sub>	1003	990	<i>a<sub>g</sub></i> v <sub>9</sub>	979	966	v <sub>9</sub>	989	977
v <sub>10</sub>	964	929	<i>a<sub>u</sub></i> v <sub>12</sub>	—	840	v <sub>10</sub>	—	954
v <sub>11</sub>	841	831	<i>a<sub>u</sub></i> v <sub>13</sub>	—	709	v <sub>11</sub>	—	795
v <sub>12</sub>	740	735	<i>a<sub>g</sub></i> v <sub>10</sub>	721	703	v <sub>12</sub>	737	726
v <sub>13</sub>	410	410	<i>a<sub>u</sub></i> v <sub>14</sub>	—	409	v <sub>13</sub>	391	377
v <sub>14</sub>	307	307	<i>a<sub>g</sub></i> v <sub>11</sub>	327	326	v <sub>14</sub>	334	323

<sup>a</sup> Unscaled wavenumbers calculated at the BLYP/6-31G\* level. <sup>b</sup> In the vapor or liquid phase (Ref. 15). <sup>c</sup> In THF (Ref. 16). <sup>d</sup> In CH<sub>3</sub>CN (Refs. 14 and 17).

C<sub>3</sub>C<sub>4</sub> bonds are lengthened on going from the neutral molecule to either the radical anion or cation. Similar structural changes have been obtained by the B3LYP and CASSCF methods. It may be concluded therefore that the removal or addition of one electron from or to biphenyl leads to changes from a benzenoid structure to a quinoid structure.

In Table 2, the unscaled vibrational wavenumbers calculated at the BLYP/6-31G\* level for biphenyl and its radical ions are compared with wavenumbers observed in the Raman spectra.<sup>14-17</sup> The *a<sub>g</sub>* and *a<sub>u</sub>* modes of the radical anion (*D*<sub>2h</sub> symmetry) are correlated to the *a* modes of the neutral species and the radical cation (*D*<sub>2</sub> symmetry). The differences between the observed and calculated wavenumbers are less than 18 cm<sup>-1</sup>, except for v<sub>10</sub> of the neutral molecule and v<sub>6</sub> of the radical cation. Such agreements between the observed and calculated wavenumbers lead to an expectation that the BLYP/6-31G\* method will be useful in assigning the vibrational spectra of the radical ions of longer *p*-oligophenyls. Sasaki and Hamaguchi<sup>14</sup> have concluded that the presence of the weak 391-cm<sup>-1</sup> band in the Raman spectrum of the radical cation results from its slightly twisted structure (*D*<sub>2</sub> symmetry). Their assignment has been confirmed by the present calculation. The calculation also shows that v<sub>6</sub> of each species is mainly due to the inter-ring C<sub>1</sub>C<sub>1</sub>' stretch. The upshifts of the inter-ring C<sub>1</sub>C<sub>1</sub>' stretch on going from the neutral molecule to the radical ions are consistent with the structural changes in the direction from benzenoid to quinoid. The calculated wavenumber of 1307 cm<sup>-1</sup> for the radical cation is 35 cm<sup>-1</sup> lower than the observed, while the calculated wavenumbers for the neutral molecule and the radical anion are in better agreement with the observed. Since the calculated length of the inter-ring C<sub>1</sub>C<sub>1</sub>' bond in the twisted structure of the

radical cation is longer than that in the planar radical anion, it seems to be natural that the calculated wavenumber for the inter-ring C<sub>1</sub>C<sub>1</sub>' stretch of the radical cation is lower than that of the radical anion. Actually, however, the wavenumber of the observed Raman band of the radical cation is significantly higher than that of the radical anion. The origin of this discrepancy between the calculated and observed wavenumbers is yet to be clarified.

We have demonstrated that the density functional theory is useful in evaluating the structures and vibrational wavenumbers of the radical anion and cation of biphenyl. We are now extending our studies to the radical anions and dianions of long-chain *p*-oligophenyls in order to gain a deeper understanding of polarons and bipolarons in nondegenerate conducting polymers.

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